8.4b Improper Integrals

Comparison Test

if
$$0 \le f(x) \le g(x)$$

and
$$\int_{a}^{\infty} f(x)dx \le \int_{a}^{\infty} g(x)dx$$

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$$\int_{1}^{\infty} e^{-x^2} dx$$

Does the integral converge or diverge?

$$\int_{1}^{\infty} \frac{dx}{x^5 + 1}$$

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Find the volume of the solid obtained by revolving the curve about the x-axis: $y=xe^{-x}$ $0 \le x < \infty$

Gabriel's Horn

Consider the region R in the fist quadrant bounded above by:

$$y = \frac{1}{x}$$
 and on the left by $x = 1$

The region is revolved around the x-axis.

- a. show the R has infinite area.
- b. Find the volume of the solid.

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