

6.5 Logistic Growth

$$\frac{dP}{dt} = kP(M - P)$$

Use the differential equation to construct a slopefield

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The growth rate of a population P of bears in a newly established wildlife preserve is modeled by the differential equation

$$\frac{dP}{dt} = .008P(100 - P) \quad \text{where } t \text{ is measured in years.}$$

- What is the carrying capacity for bears in this preserve?
- What is the bear population when the population is growing the fastest?
- What is the rate of change of the population when it is growing the fastest.

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solve the differential equation: $\frac{dP}{dt} = kP(M - P)$

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Partial fractions:

$$f(x) = \frac{5x + 4}{x^2 - 2x - 8}$$

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$$f(x) = \frac{x-13}{2x^2-7x+3}$$

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Sixty one moose were introduced to the upper peninsula in Michigan. The growth rate is given below. Solve for P

$$\frac{dP}{dt} = .0003P(1000 - P)$$

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General solution to the logistic differential equation:

$$\frac{dP}{dt} = kP(M - P)$$

$$P = \frac{M}{1 + Ae^{-(Mk)t}}$$

$$A = \frac{M - P_0}{P_0}$$

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