

39.

21. $f(x) = x^3 - 4x$ $x = -2$

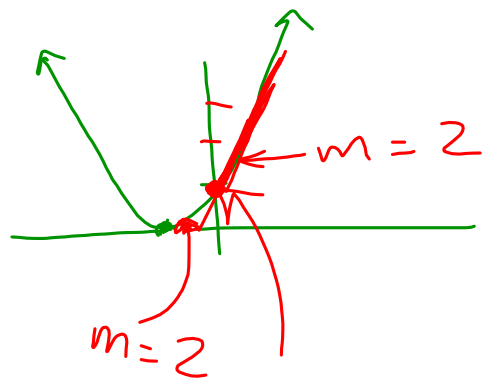
23. $f(x) = x^{\frac{2}{3}}$ @ $x=0$

27.
$$\frac{(0+h)^{\frac{2}{3}} - 0}{h} = \frac{h^{\frac{2}{3}}}{h}$$

35.
$$h^{-\frac{1}{3}} = \frac{1}{h^{\frac{1}{3}}} \cdot h^{\frac{2}{3}} = \frac{h^{\frac{2}{3}}}{h^{\frac{1}{3}}} = \frac{h^{\frac{2}{3}-\frac{1}{3}}}{h^0} = \frac{h^{\frac{1}{3}}}{1} = h^{\frac{1}{3}}$$

35.

$$g(x) = \begin{cases} (x+1)^2 & x \leq 0 \\ 2x+1 & 0 < x < 3 \\ (4-x)^2 & x \geq 3 \end{cases}$$



39.

$$f(x) = \begin{cases} 3-x & x < 1 \\ ax^2+bx & x \geq 1 \end{cases}$$

$$-2 = -a + b$$

$$-1 = 2a + b$$

$$-3 = a$$

$$5 = b$$

3.3a Rules for Differentiation

$$f(x) = 5$$

$$f'(x) = 0$$

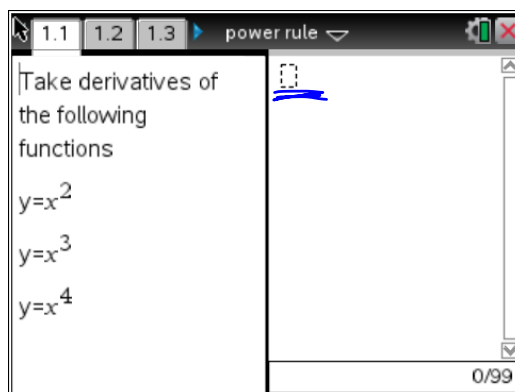
$$f(x) = -3$$

$$f'(x) = 0$$

$$\frac{d}{dx} c = 0$$

Use power rule.tns to discover the power rule for derivatives.

$$\begin{array}{l} 2x \\ 3x^2 \\ 4x^3 \end{array}$$



~~$$\frac{d}{dx} (x^n) = n \cdot x^{n-1}$$~~

$$\frac{d}{dx} (3x^4) = 12x^3$$

Proof of the Power Rule

find $\frac{dy}{dx}$ if $y = x^3 + \underline{6x^2} - \frac{5}{3}x' + 16$

$$\frac{dy}{dx} = 3x^2 + 12x - \frac{5}{3} + 0$$

$$y' = 3x^2 + 12x - \frac{5}{3}$$

$$\frac{d}{dx} \left(\frac{1}{x} \right) = \frac{d}{dx} (x^{-1}) = -1x^{-2} = -\frac{1}{x^2}$$

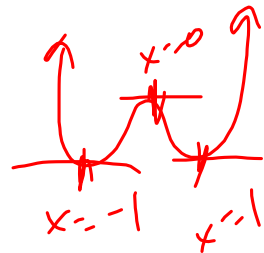
$$\frac{d}{dx} (x^{5/12}) = \frac{5}{12} x^{5/12}$$

$$\frac{d}{dx} (x^{2/5}) = \frac{2}{5} x^{-3/5} = \frac{2}{5x^{3/5}}$$

find horizontal tangent of

$$y = x^4 - 2x^2 + 2$$

$$y' = 4x^3 - 4x = 0$$



$$4x(x^2 - 1) = 0$$

$$4x(x+1)(x-1) = 0$$

$$x = -1, 1, 0$$

higher order derivatives:

$$y = x^4 - 2x^2 + 2$$

$$y' = 4x^3 - 4x$$

velocity

$$y'' = 12x^2 - 4$$

acceler.

$$y''' = 24x$$

jerk